

FINAL EXAM FOR MTH102 SPRING007

THE 102 TEAM : AYMAN, MARWAN, LEDUC, LUIS, TOM, YUSUF, ZAYID

Name _____, Id. Num. _____, Score $\overline{100}$

QUESTION 1. (20 points, each = 5 points)

SHOW WORK TO RECEIVE FULL CREDIT BUT DO NOT SIMPLIFY YOUR ANSWER

(1) Find each of the following:

(a) $f(x) = (\ln(x^3 - 2x + 1))^8$
 $f'(x) =$

(b) $f(x) = \frac{e^{x^2}}{x + e^x}$
 $f'(x) =$

(c) $f(x, y) = xe^y + ye^x$
 $f_x(x, y) =$

$f_{xy}(x, y) =$

(d) $f(x) = 10^{2x} \ln(x + x^{-2})$
 $f'(x) =$

QUESTION 2. (18 points, each = 6 points)

$$(1) \int_1^2 \frac{x^3 e^{-x} - 3 + x^2}{x^3} dx =$$

$$(2) \int x(x^2-9)^4 dx =$$

$$(3) \int \frac{x^2 - 10x + 7}{(x^3 - 15x^2 + 21x + 8)} dx =$$

QUESTION 3. (10 points) (4) The marginal average cost for producing x fuel-cell cars is given by $-\frac{2,000,000}{x^2}$ and the average cost of producing 1000 vehicles is \$27,000 per vehicle. Find the marginal cost $C'(x)$ and evaluate it for a production of 2000 vehicles. (Hint: As a first step, Find the AVERAGE COST)

QUESTION 4. (10 points) Find Local Min. and Local max., if any, for $f(x) = -x^3 + 6x^2 - 9x$.

QUESTION 5. (12 points) Let x be the number of units from product A, and y be the number of units from product B. Given the total profit function $P(x, y) = xy + x^2 + y^2 - 90x - 60y + 100$. For what values of x and y will the profit be maximum? What is the maximum profit?

QUESTION 6. (10 points) Sketch the graph of $f(x)$ that satisfy the following conditions:

- 1) $f(-2) = 1, f(0) = 0, f(2) = 1$.
- 2) $f'(0) = 0, f'(x) < 0$ on the interval $(-\infty, 0), f'(x) > 0$ on the interval $(0, \infty)$
- 3) $f''(-2) = 0, f''(2) = 0$.
- 4) $f''(x) > 0$ on the interval $(-2, 2)$ and $f''(x) < 0$ on the interval $(-\infty, -2) \cup (2, \infty)$
- 5) $\lim_{x \rightarrow -\infty} f(x) = \lim_{x \rightarrow \infty} f(x) = 2$

QUESTION 7. (5 points) a) Find all the horizontal and vertical asymptotes of $\frac{x^2+x-6}{2x^2-18}$.

(8 points) b) Find the equation of the tangent line to the curve $x^2 - y = 4e^y$ at the point $(2, 0)$

(7 points) c) Let x be the number of units from product A , and p be the selling price per unit. If $x = f(p) = \frac{50}{p} - p + 15$.

a) Find the elasticity at $p = 5$.

b) If the 5 dollars price changes by 20%, use part (a) to approximate the change in demand.